

Google's tile engine explained

Google is holding the world in a number of 256×256 pre-rendered images ("tiles") for about 18 zoom stages. The lowest zoom is 0, the highest 17. Every point - hmm, nearly every with the exception of the pole area - on earth can be found in exactly one tile at any zoom.

At zoom 0 the entire world is kept in one single tile. At zoom 17 the world spreads over giant 17.179.869.184 tiles.

The number of tiles needed to cover the entire world for a zoom stage can be calculated with

$$\text{NrOfTiles} = 2^{\text{pow}(2 * \text{Zoom})}$$

With every increment of the zoom the width/height of the bitmap doubles, so the image area size is multiplied by 4 each time. The origin of the resulting bitmap (0, 0) is in the top/left corner. The center coordinate is always equivalent to the earth geo code (0, 0). One could imagine this simple behaviour as some sort of "video projection" onto a surface: If you are very close to the projector the image may be captured on a single sheet of paper. If you increase the distance between the projector and your paper, you'll obviously have to enlarge the sheet or paste a bunch of papers together in order capture the whole projector image.

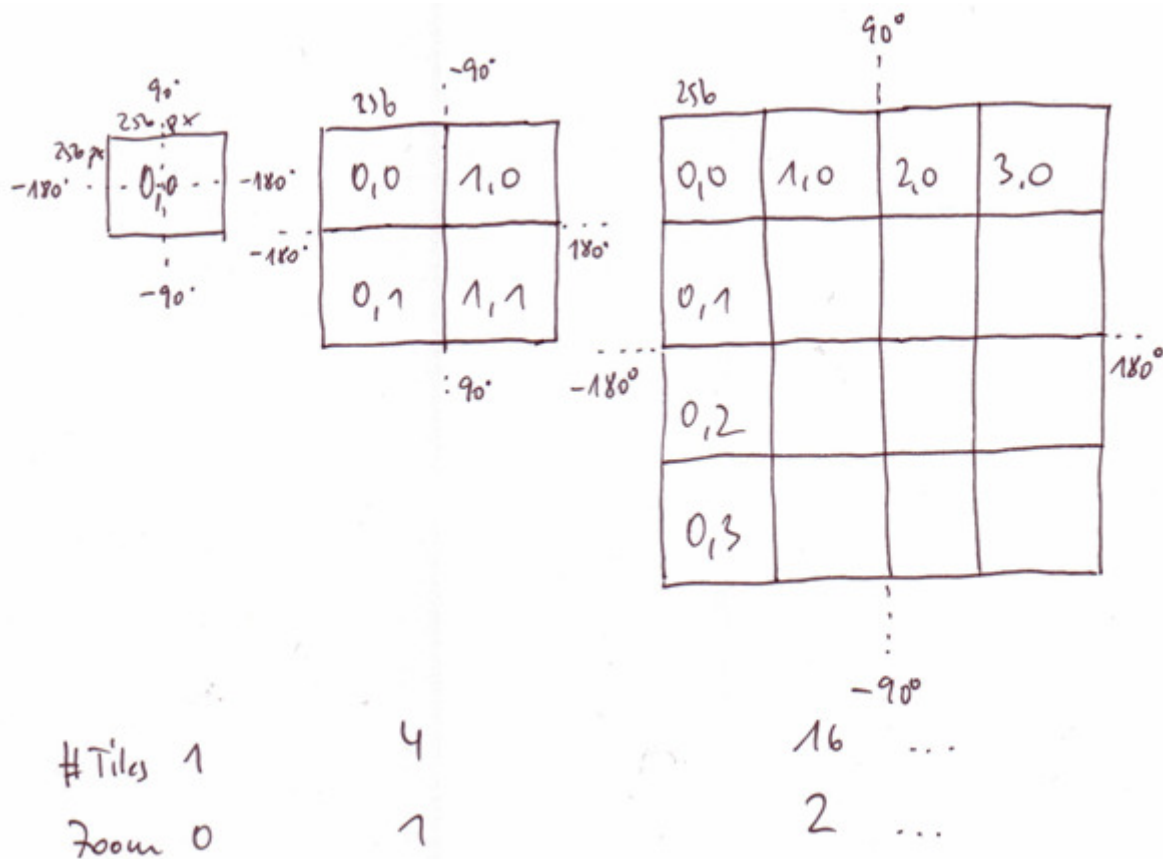


Fig. 1: Basic principles of Google's mapping and sample tile coordinates

Google is using Mercator projection. There is a couple of algorithms out in order to determine bitmap pixel coordinates for a given geo coordinate and zoom stage, so the following is not the only, but a simple and easy to understand solution of the problem.

$$x = \lambda - \lambda_0$$

$$\lambda_0 = \text{lon in center of map}$$

$$y = \frac{1}{2} \ln \left(\frac{1 + \sin(\phi)}{1 - \sin(\phi)} \right)$$

$$\phi = \text{lat}$$

Fig. 2: Basic Mercator formulas to calculate X and Y coordinates in a map for a given longitude lambda and latitude phi (http://en.wikipedia.org/wiki/Mercator_projection)

The following C# code uses the formulas of Fig. 2 in order to calculate X and Y for a lat/lon/zoom.

```
public class TileCoordinate {
    public TileCoordinate(double row, double column, int zoom) {
        this.row = row;
        this.column = column;
        this.zoom = zoom;
    }
    public double row;
    public double column;
    public int zoom;
}

static TileCoordinate locationCoord(double lat, double lon, int zoom) {
    if (System.Math.Abs(lat) > 85.0511287798066)
        return null;
    double sin_phi = System.Math.Sin(lat * System.Math.PI / 180);
    double norm_x = lon / 180;
    double norm_y = (0.5 * System.Math.Log((1 + sin_phi) / (1 - sin_phi))) / System.Math.PI;
    double tileRow = System.Math.Pow(2, zoom) * ((1 - norm_y) / 2);
    double tileColumn = System.Math.Pow(2, zoom) * ((norm_x + 1) / 2);
    return new TileCoordinate(tileRow, tileColumn, zoom);
}
```

Earth geo coordinates vary in the range of

-90° <= latitude <= 90° and
-180° <= longitude <= 180°

Mercator is per definition not applicable for geo coordinates above +/- 85.0511287798066, because the y calculation tends to reach a singularity at 90 degrees. The algorithm checks for those "invalid" coordinates.

After calculating X and Y according to the Mercator formulas X and Y are normalized by the algorithm to fit into the interval

-1 <= x <= 1 and
-1 <= y <= 1

by dividing by 180 (X) respectively PI (Y).

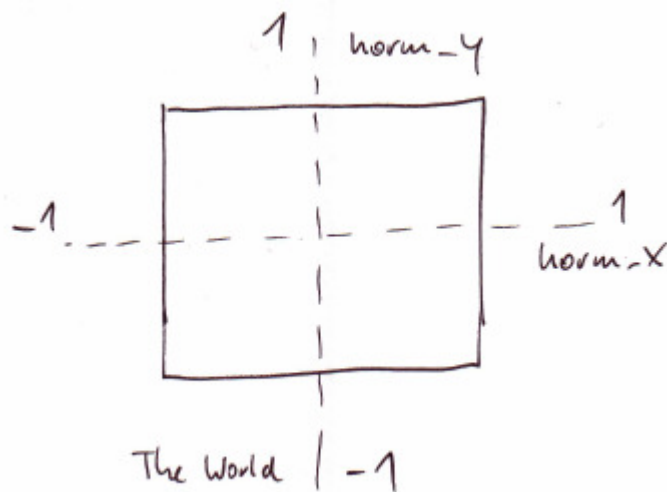


Fig. 3: Normalized X and Y

The resulting values `norm_x` and `norm_y` may then be applied to any kind of square mapping. In the above code it is applied to match Google's world projection as shown in Fig. 1. The result is a row/column/zoom tuple, which may be used to query Google's "keyhole" map servers in order to obtain the images. The `floor(x)` and `floor(y)` values may be used directly as parameters for the query. The zoom parameter in the query has to be set to 17-zoom. The fraction of `x` and `y` multiplied with 256 give the relative coordinates within a tile.

Sample: Geocode of center of Berlin/Germany 52.5211° 13.4122° at zoom 10

`x = 550`
`y = 335`

Query:

`http://mt.google.com/mt?x=550&y=335&zoom=7`

If one has to ask for a couple of tiles in parallel in order to build up a larger image, it is sometimes more efficient to spread this task over multiple threads, using the 4 keyhole servers in a pseudo-random manner.

E.g. one query goes to <http://mt0.google.com/mt>, another to `mt1` and so on.

Note:

Google Maps for Mobile uses 64*64 tiles instead of 256*256 for optimization reasons. Therefore the resulting `TileCoordinate` has to be multiplied with 4 in its row and column part to fit the needs. Furthermore there is another URL and mechanism to retrieve the images. For details see the sample code at <http://maps.alphadex.de>